



Измерение спектральной функции  $\tau$ -лептона  
в распаде  $\tau^- \rightarrow K^- K_S^0 \nu_\tau$  в эксперименте BaBar













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22 июня 2018 г.



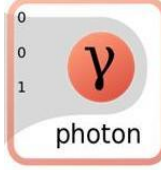
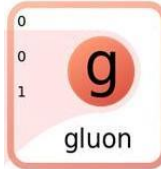
# Fundamental particles

Matter ↓ s=1/2      Field ↓ s=1

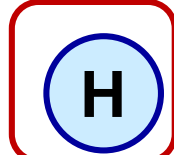
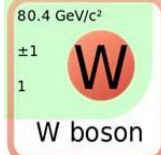
|             | 1st gen.   | 2nd gen.   | 3rd gen.   |
|-------------|--|--|--|
| Q U A R K   | <br><i>u</i><br>up                            | <br><i>c</i><br>charm                         | <br><i>t</i><br>top                           |
|             | <br><i>d</i><br>down                          | <br><i>s</i><br>strange                       | <br><i>b</i><br>bottom                        |
| L E P T O N | <br><i>ν<sub>e</sub></i><br><i>e neutrino</i> | <br><i>ν<sub>μ</sub></i><br><i>μ neutrino</i> | <br><i>ν<sub>τ</sub></i><br><i>τ neutrino</i> |
|             | <br><i>e</i><br>electron                     | <br><i>μ</i><br>muon                         | <br><i>τ</i><br>tau                          |



**Flavors**



$r < 10^{-17}$  cm !



s=0      125 GeV

+3 colours for each quarks

3 generations  
+ antiparticles

Total number : 60 + H = 61

All have spin excl H

**M(matter) ~ 550 GeV**

$\Sigma Q(\text{quarks}) = - \Sigma Q(\text{leptons}) !$

Что такое спектральная функция (SF);  $\tau^- \rightarrow K^- K_S^0 \nu_\tau$

$$V(m) = 2 \frac{1}{N} \frac{dN}{dm} \frac{1}{m(M_\tau^2 - m^2)^2 (M_\tau^2 + 2m^2)} \frac{B(\tau \rightarrow K_S K \nu)}{B(\tau \rightarrow e \nu \nu)} \frac{M_\tau^6}{12\pi V_{ud}^2}$$

$V(m)$  описывает спектр масс адронов в распаде  $\tau$ :  $dN/dm (K^- K_S)$

Согласно CVC SF связывает спектр масс  $dN/dm$  с сечением  $e^+e^-$

$$V(m) = \frac{m^2}{4\pi^2 \alpha^2} \sigma_{e^+e^- \rightarrow K \bar{K}(I=1)}(m)$$

## Мотивация данной работы:

✓ Измерение спектральной функции (SF) в распаде  $\tau^- \rightarrow K^- K_S \nu_\tau$

✓ Используя CVC и SF получить изовекторный вклад в сечение  $e^+e^- \rightarrow K Kbar (I=1)$



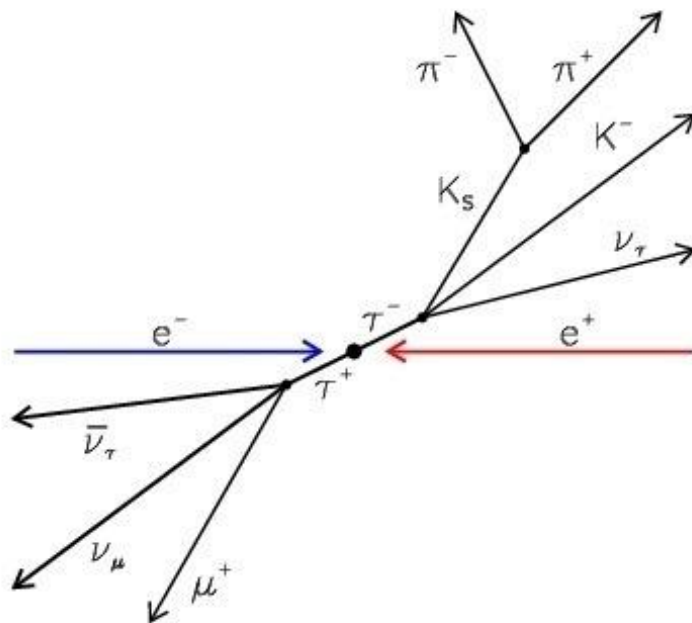
✓ Сравнить расчетные изовекторные вклады от  $e^+e^-$  и  $\tau$  для процессов  $e^+e^- \rightarrow K Kbar (I=1)$

✓ Корректировка массового спектра в MC генераторе  $\tau \rightarrow K^- K_S \nu_\tau$

# $\tau$ – lepton production at BaBar

$$e^+e^- \rightarrow \tau^+ \tau^-$$

$$E_{\text{c.m.}} = m(Y(4S)) = 10.58 \text{ GeV}$$



$$\sigma_{\tau\tau} = 0.92 \text{ nb}$$

$$L \approx 0.5 \text{ ab}^{-1}$$

$$N_{\tau\tau} \approx 10^9$$

## $\tau$ Branching Ratios (PDG 2016)

$$\begin{aligned} \text{BR}(\tau^- \rightarrow K_S K^- \nu_\tau) &= 0.740 \pm 0.025 \cdot 10^{-3} \\ \text{BR}(\tau^- \rightarrow K_S \pi^- \nu_\tau) &= 4.2 \pm 0.07 \cdot 10^{-3} \\ \text{BR}(\tau^- \rightarrow K_S K^- \pi^0 \nu_\tau) &= 0.75 \pm 0.04 \cdot 10^{-3} \\ \text{BR}(\tau^- \rightarrow K^- \nu_\tau) &= 0.696 \pm 0.01 \% \\ \text{BR}(\tau^- \rightarrow \pi^- \nu_\tau) &= 10.82 \pm 0.05 \% \end{aligned}$$

## $\tau$ Branching Ratio in MC

$$\text{BR}(\tau^- \rightarrow K_S K^- \nu_\tau) = 0.8255 \cdot 10^{-3}$$

11.5% difference !

# CLEO $K^+K_S^-$ mass spectrum from $\tau$ decay.

CLEO Collab. Phys.Rev.D 53, 6037 (1996)

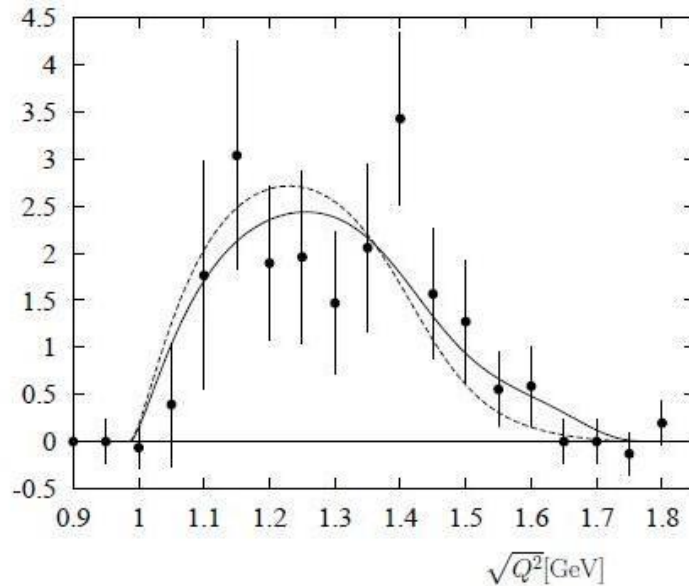


Figure 7: The normalized distribution  $\frac{d\Gamma(\tau \rightarrow K^- K^0 \nu_\tau)/d\sqrt{Q^2}}{\Gamma(\tau \rightarrow K^- K^0 \nu_\tau)}$  in the kaon pair invariant mass  $\sqrt{Q^2}$  in units of  $\text{GeV}^{-1}$  obtained from the fitted kaon form factor; the solid (dashed) line corresponds to the constrained (unconstrained) fit. The event distribution measured by CLEO Collaboration [45] and normalized, dividing by the total number of events, is shown with points.

## DATA used in analysis

1. Run1-run6 - 468.3 fb<sup>-1</sup>  
kL=L<sub>MC</sub> /Lrun
2. MC e<sup>+</sup>e<sup>-</sup> → τ<sup>+</sup>τ<sup>-</sup> , 816.3 fb<sup>-1</sup> , kL = 1.74
3. MC e<sup>+</sup>e<sup>-</sup> → τ<sup>+</sup>τ<sup>-</sup> → l<sup>+</sup>K<sub>S</sub>K<sup>-</sup>ν<sub>τ</sub>, 1088 fb<sup>-1</sup> , kL = 2.32
4. MC e<sup>+</sup>e<sup>-</sup> → uds , 856 fb<sup>-1</sup> , kL= 1.83
5. MC e<sup>+</sup>e<sup>-</sup> → c-cbar , 868.5 fb<sup>-1</sup> , kL= 1.85
6. MC e<sup>+</sup>e<sup>-</sup> → B-Bbar, 1352.4 fb<sup>-1</sup> , kL= 2.89



## Selection criteria

$$\tau_1 \rightarrow \text{KK}_S, \tau_2 \rightarrow e\nu\nu, \mu\nu\nu$$

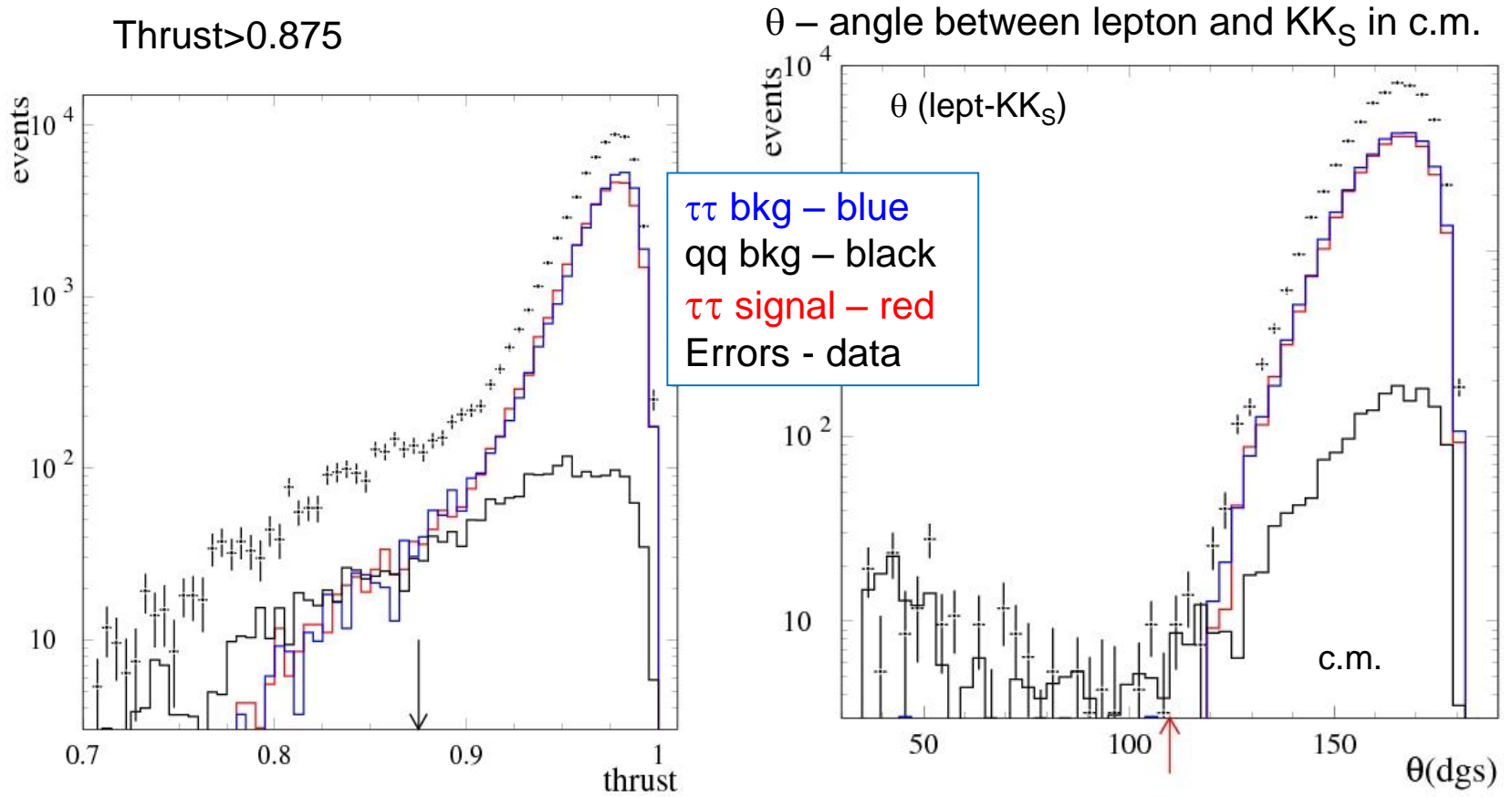
1.  $N(\text{tracks})=4$ ,
2.  $N(\text{K}_S)=1$ ,  $\text{K}_S \rightarrow \pi^+\pi^-$
3.  $N(\text{K}^\pm)=1$ ,  $N(\mu)$ .or. $N(e)=1$
4.  $r_{\text{KS}} = 1 - 70 \text{ cm}$
5.  $\text{thrust} > 0.875$
6.  $\text{K}^\pm : p_{\text{lab}} = 0.4-5$ ,
7.  $e, \mu : \cos\theta_{\text{lab}} < 0.9$ ,  $p_{\text{lab}} > 1.2$ ,  $p_{\text{cm}} < 4.5$
8.  $\theta_{\text{CM}} > 110^\circ$ , - angle lept.  $\leftrightarrow \text{KK}_S$
9.  $\Sigma E_\gamma < 2 \text{ GeV}$

## Monte carlo selection of

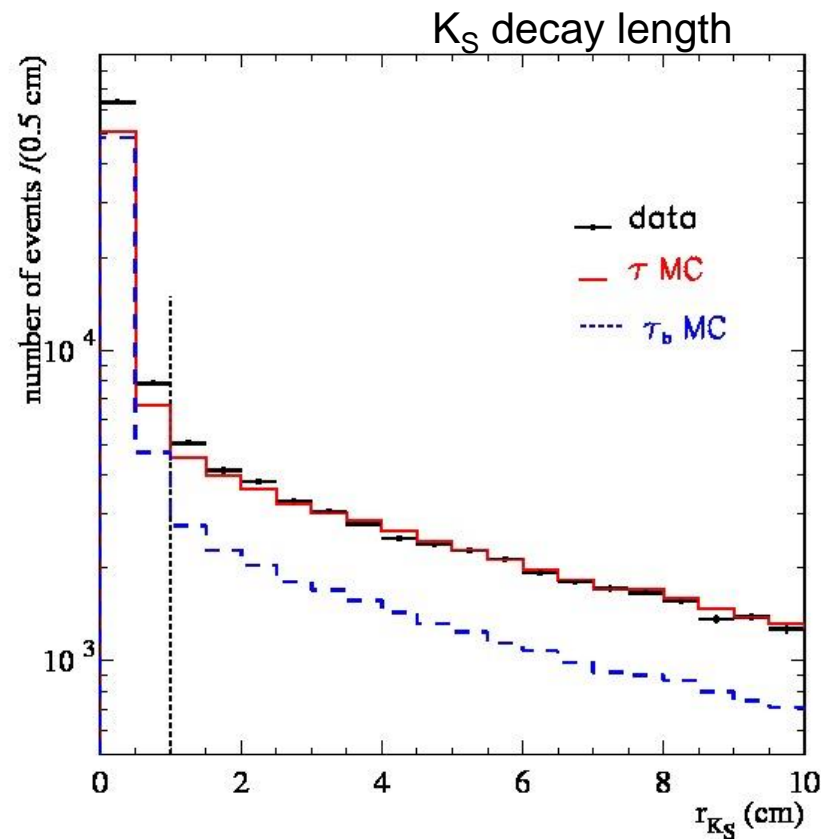
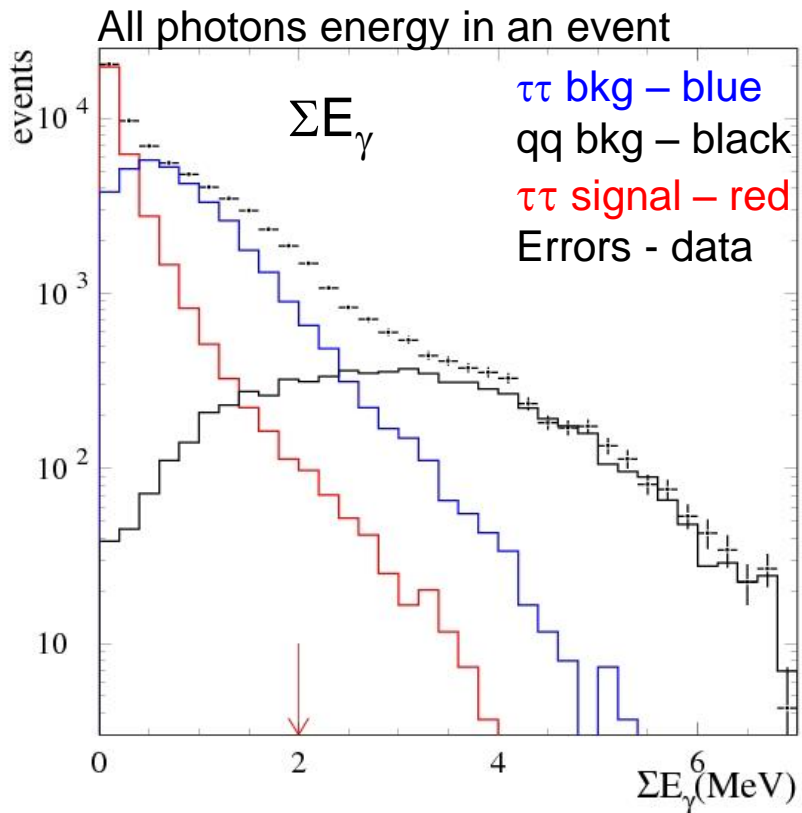
$\tau^+\tau^- \rightarrow l^+\text{K}_S\pi^-\nu_\tau$  mode :

1.  $N(\text{K}_S)=1$ ,  $N(\text{K}^\pm)=1$
2.  $N(\mu)$ .or. $N(e)=1$
3.  $N(\pi^0)=0$ ,  $N(\pi^\pm)=0$

# Comments to selection conditions



# Comments to selection conditions



## Signal and background suppression - all cuts applied

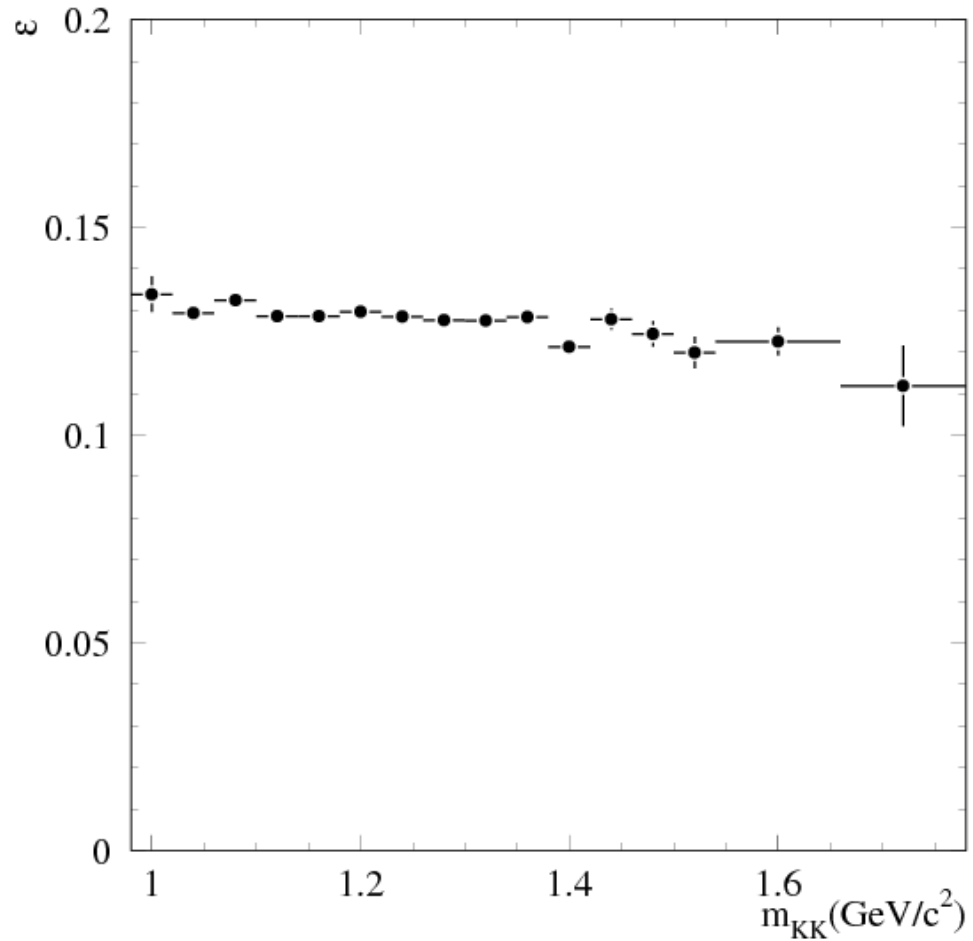
$\tau+\tau-(MC) \sim 7.5 \cdot 10^8 \text{ ev.} \rightarrow 1.2 \cdot 10^5 \text{ ev.} \text{ (} \sim 3.5 \text{ orders)}$

$udscb(MC) \sim 4.3 \cdot 10^9 \text{ ev.} \rightarrow 3.5 \cdot 10^3 \text{ ev.} \text{ (} \sim 6 \text{ orders)}$

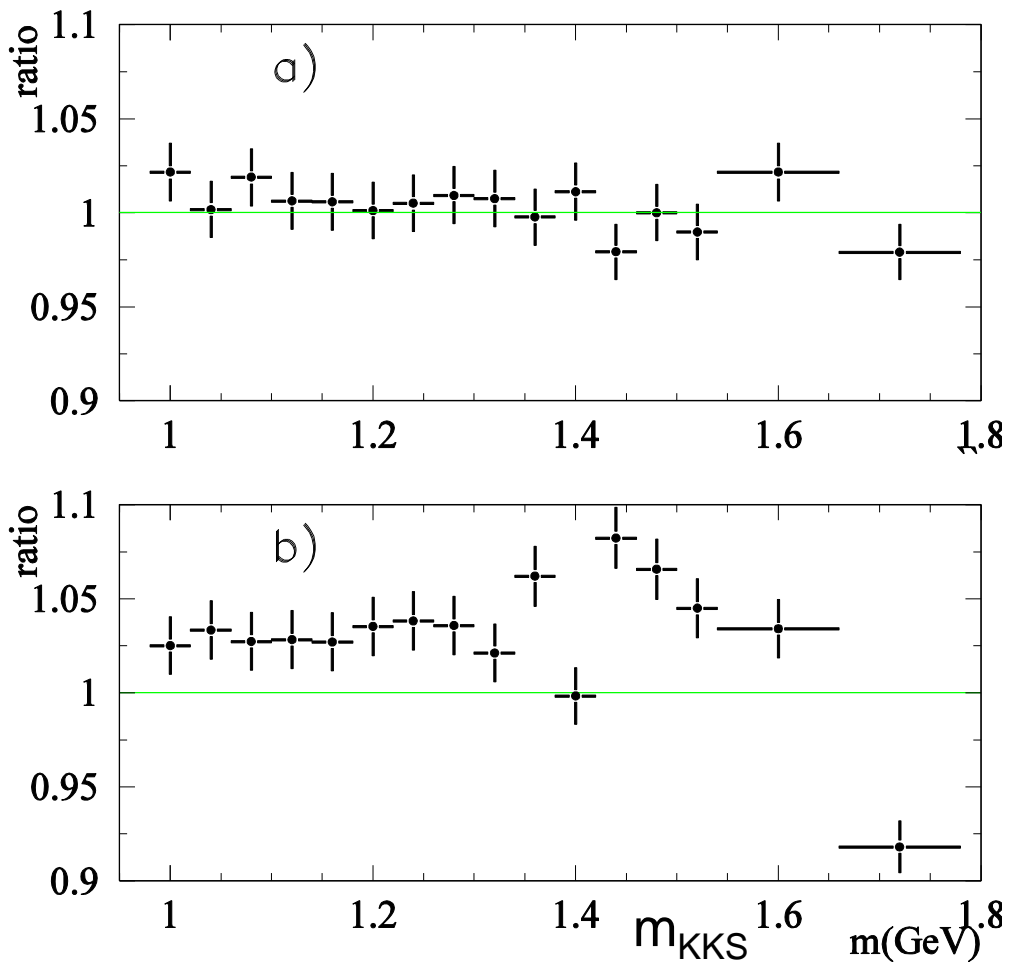
$\tau+\tau-(KK_S,MC) \sim 3 \cdot 10^5 \text{ ev.} \rightarrow 0.7 \cdot 10^5 \text{ ev} \text{ (} \sim 4 \text{ times)}$

$\text{data} \quad \sim 4.2 \cdot 10^9 \text{ ev.} \rightarrow 1.4 \cdot 10^5 \text{ ev} \text{ (} \sim 4.5 \text{ order)}$

## Detection efficiency vs $KK_S$ mass – all cuts applied



# Data/MC efficiency corrections



- a) – signal  $\tau \rightarrow KK_S \nu_\tau$
- b) – non  $\tau \rightarrow KK_S \nu_\tau$

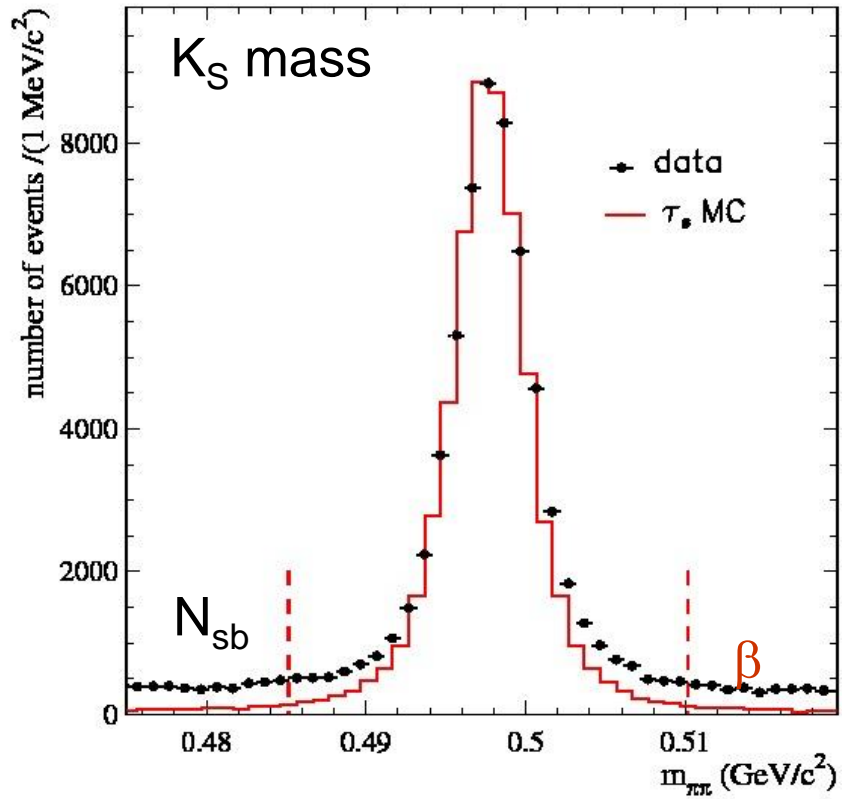
Used PID Tables from:  
 muSelectorsMap(21)  
 KselectorsMap(26)  
 eSelectorsMap(8)

Corrected MC efficiencies:

$K \rightarrow K, \pi \rightarrow K$   
 $\mu \rightarrow \mu, \pi \rightarrow \mu$   
 $e \rightarrow e, \pi \rightarrow e$

Corrections applied  
 to value of  $\varepsilon$   
 in previous slide

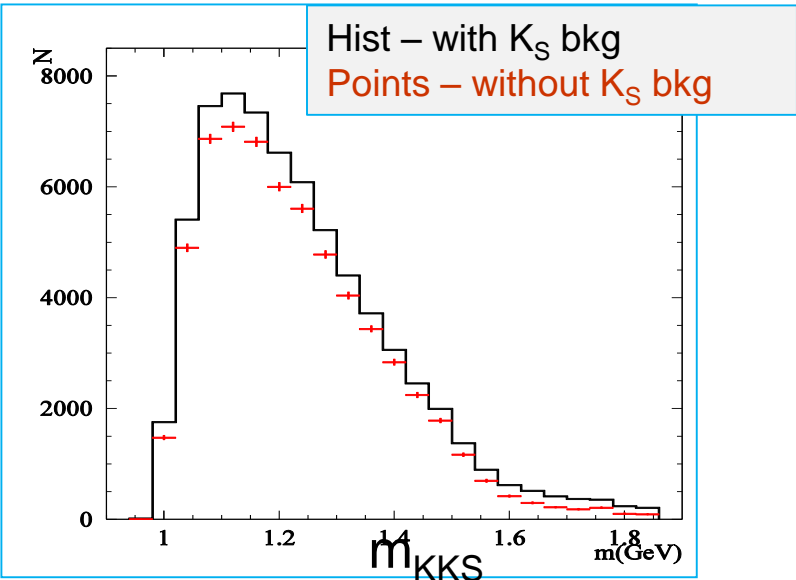
# K<sub>S</sub> background subtraction



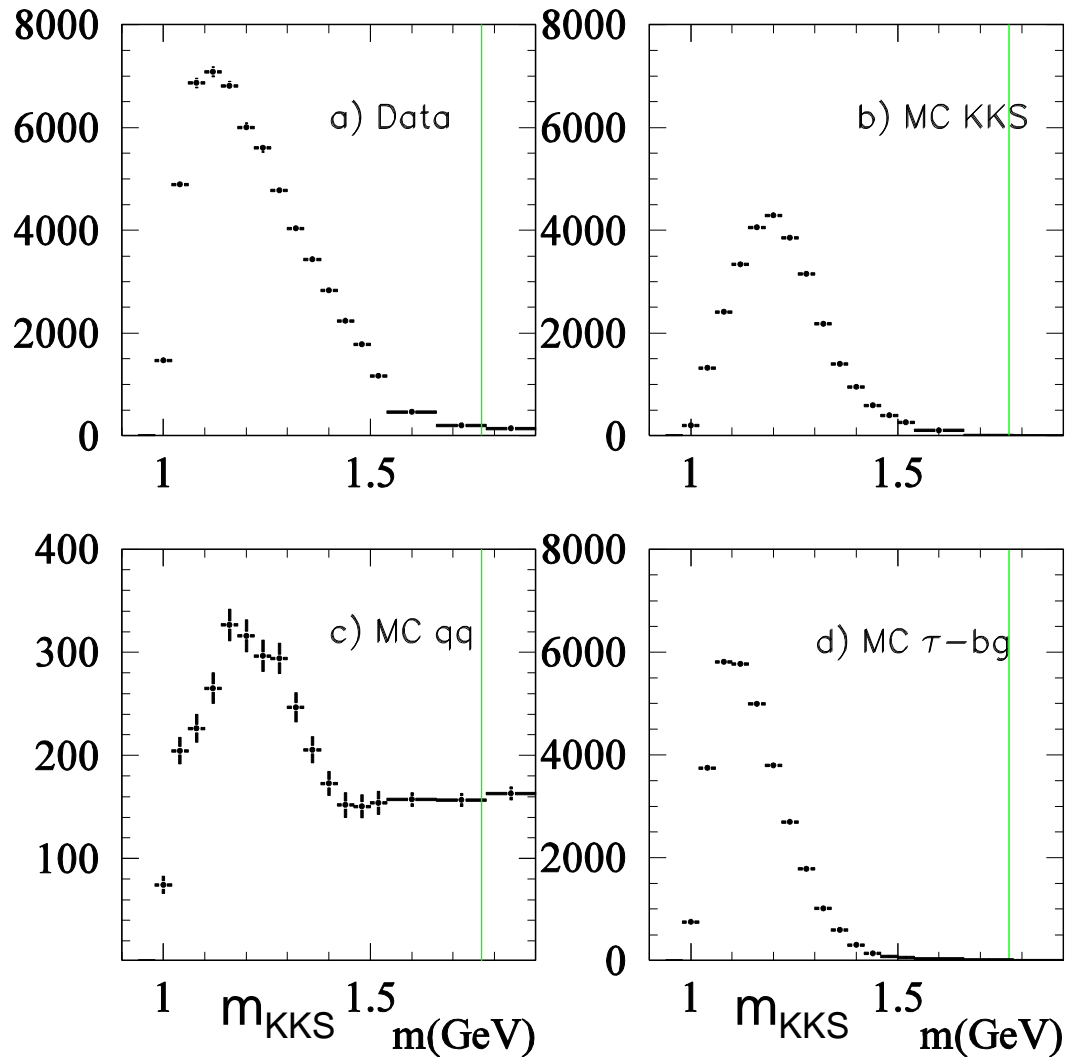
Δm=0.472-0.522=0.050 GeV

Effect of K<sub>S</sub> background subtraction

Sideband subtraction  
 $N_{KS} = (\alpha N - N_{sb}) / (\alpha - \beta)$   
 $\alpha = 0.5, \beta = 0.0315$

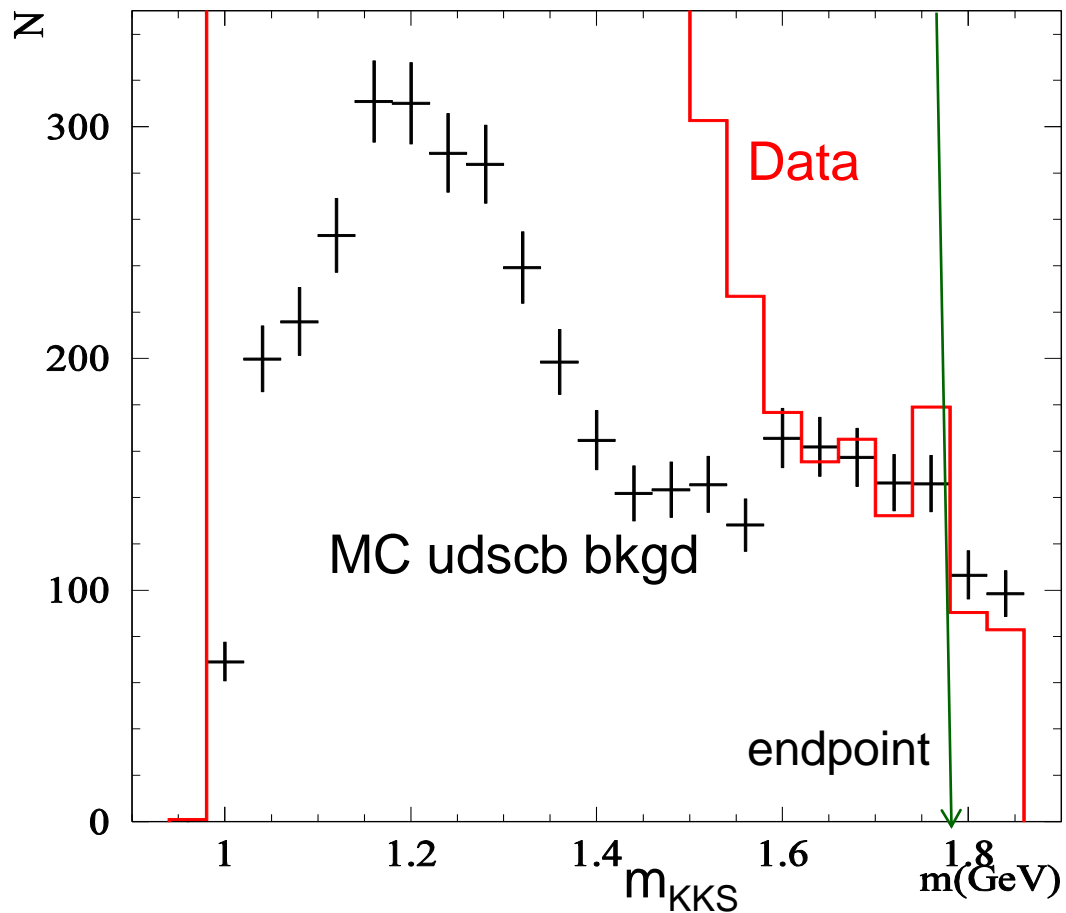


KK<sub>S</sub> mass spectra in data and MC after applying selection cuts. K<sub>S</sub> bkgd subtracted



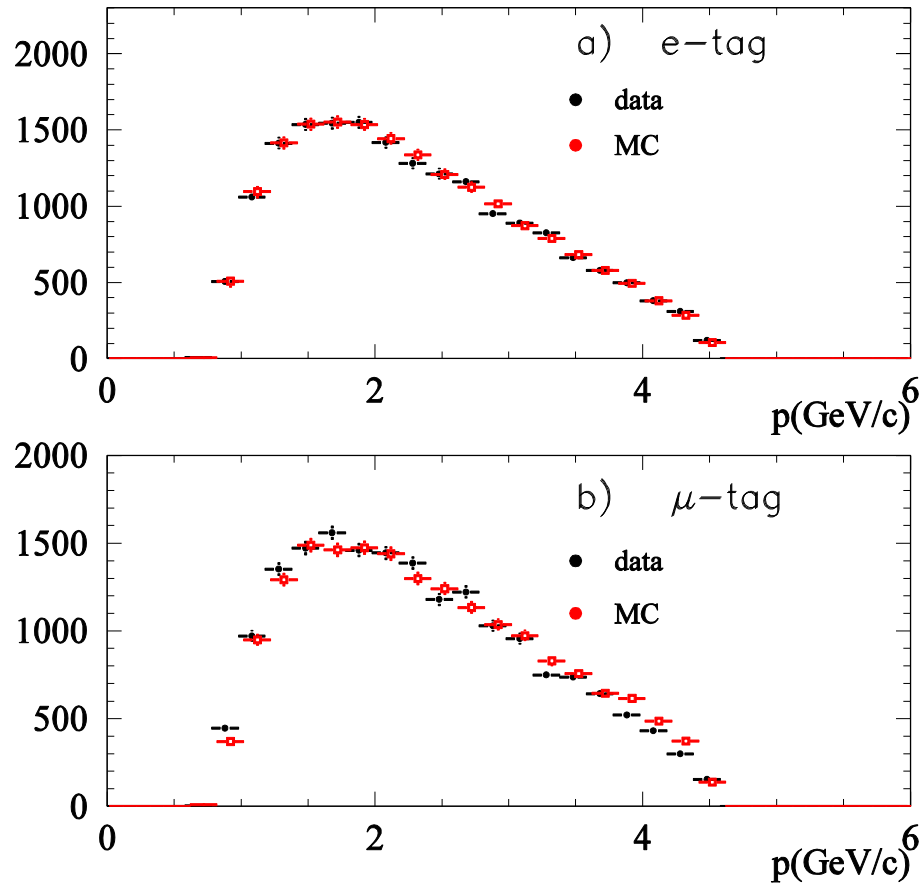


# $q\bar{q}$ background contribution



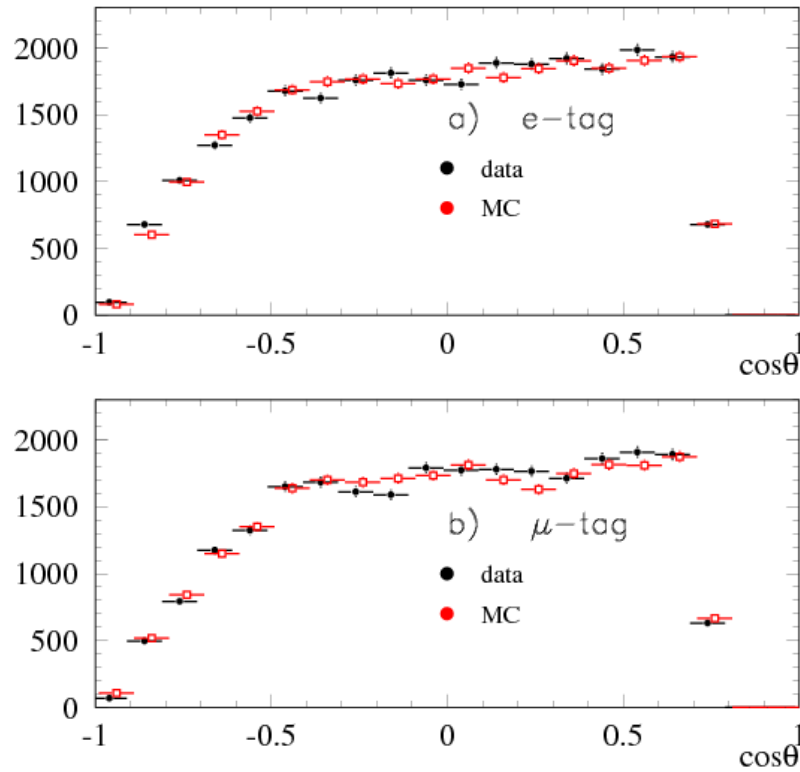
Data agree with MC near endpoint at  $m(KK_S) \sim m(\tau)$  !

# Lepton CM momentum, data-MC comparison



$q\bar{q}$  background  
subtracted from data

# Leptons CM $\cos\theta$ , data-MC comparison



$q\bar{q}$  background  
subtracted from data

## Distribution of selected events over subprocesses

Data events  
number (69286 ev.)

Tau MC  $\tau^+\tau^- \rightarrow l\bar{K}_S K^+$   
events number (32341 ev.)

+

Tau MC  $\tau^+\tau^- \rightarrow \text{non } l\bar{K}_S K^+$   
events number (35441 ev.)

+

MC hadron bkgd  
 $e^+e^- \rightarrow \text{udscb}$   
events number (5382 ev.)

## Structure of $\tau$ background

- |    |  |  |
|----|--|--|
| 1. | $\tau^- \rightarrow K_S K^- \pi^0 \nu_\tau \sim 70\%$  | Background without $\pi^0$ , well measured, subtracted using MC                      |
| 2. | $\tau^- \rightarrow \pi^- K_S \nu_\tau \sim 10\%$      |  |
| 3. | $\tau^- \rightarrow \pi^- K_S \pi^0 \nu_\tau \sim 6\%$ | Background with $\pi^0 \sim 80\%$ , mass spectra not measured, subtracted using data |
| 4. | $\tau^- \rightarrow \pi^- \nu_\tau \sim 8\%$           |  |
| 5. | $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$              |  |

## Structure of qq background

uds  $\sim 80\%$  , cc  $\sim 15\%$ , bb  $\sim 5\%$

# Subtraction of $\pi^0$ background

## System of linear equations (in each $KK_S$ mass bin)

Eq.1

$$N_{ex0} = (1 - \epsilon_S) N_{sig}^\tau + (1 - \epsilon_b) N_{bg}^\tau$$

$$N_{ex1} = \epsilon_S N_{sig}^\tau + \epsilon_b N_{bg}^\tau$$

$N_{\pi^0} = 0$ ,  
number of found  $\pi^0$

$$\begin{aligned} N_{ex0} &= N_{dt0} - N_{bg,0}^{\tau,0} - N_{qq0} \\ N_{ex1} &= N_{dt1} - N_{bg,1}^{\tau,0} - N_{qq1} \end{aligned}$$

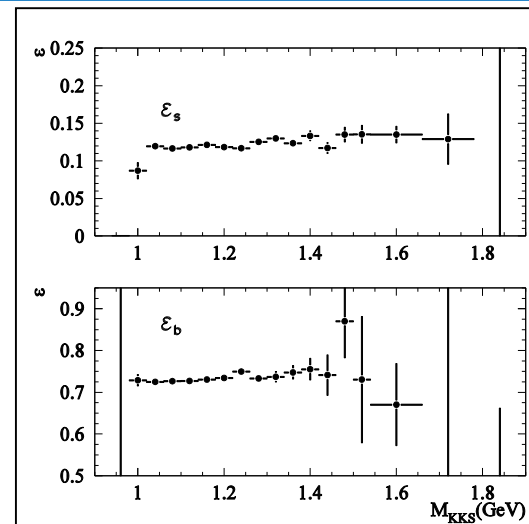
Eq.2

$$\begin{aligned} \epsilon_S &= N_{sig,1}^{\tau,0} / (N_{sig,1}^{\tau,0} + N_{sig,0}^{\tau,0}) \\ \epsilon_b &= N_{bg,1}^{\tau>0} / (N_{bg,1}^{\tau>0} + N_{bg,0}^{\tau>0}) \end{aligned}$$

Eq.3

Solution of linear equations gives the signal ( $N_{KS}^\tau$ ) and background ( $N_{bg}^\tau$ )  $KK_S$  mass spectra

← From MC



Correction to  $\pi^0$  efficiency:

$$\begin{aligned} \delta\epsilon &= 1 - (0.024 \pm 0.008) = \\ &= 0.976 \pm 0.008 \\ &\text{(BAD 2621)} \end{aligned}$$

$$\epsilon_S \neq 0$$

Extraction of KKS mass spectrum from the system of linear equations (in each  $KK_S$  mass bin)

Eq.1

$$N_{ex0} = (1 - \epsilon_S) N_{sig}^\tau + (1 - \epsilon_b) N_{bg}^\tau$$

$$N_{ex1} = \epsilon_S N_{sig}^\tau + \epsilon_b N_{bg}^\tau$$

Solution of linear equations gives the signal ( $N_{KS}^\tau$ ) and background ( $N_{bg}^\tau$ )  $KK_S$  mass spectra

Correction to  $\pi^0$  efficiency:

$$\begin{aligned} \delta\epsilon &= 1 - (0.024 \pm 0.008) = \\ &= 0.976 \pm 0.008 \\ &\text{(BAD 2621)} \end{aligned}$$

$$\epsilon_S \neq 0$$

$N_{\pi^0} = 0$ ,  
number of found  $\pi^0$

Eq.2

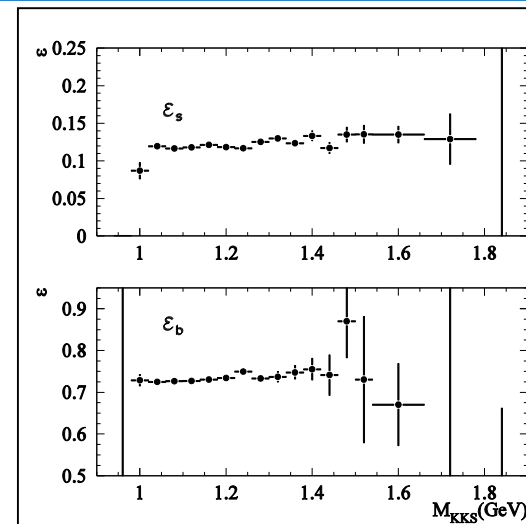
$$\begin{aligned} N_{ex0} &= N_{dt0} - N_{bg,0}^{\tau,0} - N_{qq0} \\ N_{ex1} &= N_{dt1} - N_{bg,1}^{\tau,0} - N_{qq1} \end{aligned}$$

$$\epsilon_S = N_{sig,1}^{\tau,0} / (N_{sig,1}^{\tau,0} + N_{sig,0}^{\tau,0})$$

$$\epsilon_b = N_{bg,1}^{\tau>0} / (N_{bg,1}^{\tau>0} + N_{bg,0}^{\tau>0})$$

Eq.3

From MC



# Subtraction of $\pi^0$ background

## Structure of $\pi^0$ background

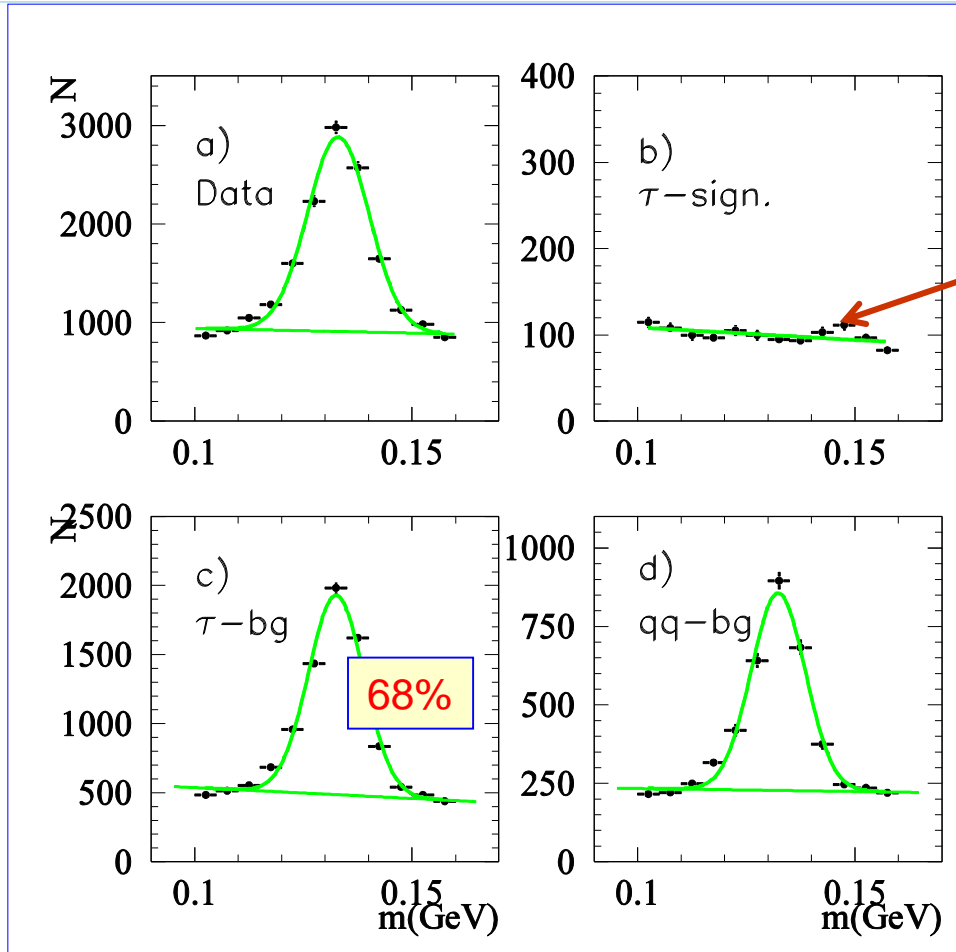
$\pi^0$  spectra for sum of events in all  $\Delta m$  bins

$$M(\pi^0) = M_{\gamma\gamma} = 100-160 \text{ MeV}$$

Fitting gives:

$$N_{\pi^0} = N_{\text{GAUSS}} + N_{\text{RANDOM}}$$

Only  $N_{\text{RANDOM}}$



68% - is the part of events with true  $\pi^0$  in  $\tau$  background



Split lower line in Eq.1 p.24 (for sum of events)

## Transformation of lin.equations

$$N_{\text{ex0}} = (1 - \varepsilon_S) N_{\text{sig}}^\tau + (1 - \varepsilon_b) N_{\text{bg}}^\tau$$

$$N^0_{\text{ex1}} = \varepsilon_S N_{\text{sig}}^\tau + 0.32 \cdot \varepsilon_b N_{\text{bg}}^\tau$$

Without true  $\pi^0$

$$N^*_{\text{ex1}} = \dots\dots\dots 0.68 \cdot \varepsilon_b N_{\text{bg}}^\tau$$

With true  $\pi^0$

# Corrections to background subtraction (for sum of events in all $\Delta m$ bins )

## Ideal equation system

$$N_{ex0}^* = N_{sig}^\tau + (1 - \epsilon_b^*) N_{bg}^\tau$$

$$N_{ex1}^* = \epsilon_b^* N_{bg}^\tau$$

$N_{ex0}^*$  – events without  $\pi^0$  + lin. background

$N_{ex1}^*$  – events with  $\pi^0$  from Gaussian fit to the  $\pi^0$  spectrum only

$$N_{sig}^\tau \text{ (modified)} = 1.01 N_{sig}^\tau \text{ (p.24)}$$

$$\epsilon_s^* = 0!$$
$$\epsilon_b^* \rightarrow 0.68 * 0.72 = 0.49$$

Fraction of events with  $\pi^0$

Return to eq,1 p.24 with division into  $KK_S$  mass bins with corrected efficiencies

$$N_{\text{ex0}} = (1 - \varepsilon'_S) N_{\text{sig}}^\tau + (1 - \varepsilon'_b) N_{\text{bg}}^\tau$$

$$N_{\text{ex1}} = \varepsilon'_S N_{\text{sig}}^\tau + \varepsilon'_b N_{\text{bg}}^\tau$$

**Corrected efficiencies:**

$\varepsilon'_S \rightarrow \varepsilon_S (1.05 \pm 0.05)$

$\varepsilon'_b \rightarrow \varepsilon_b 0.984$

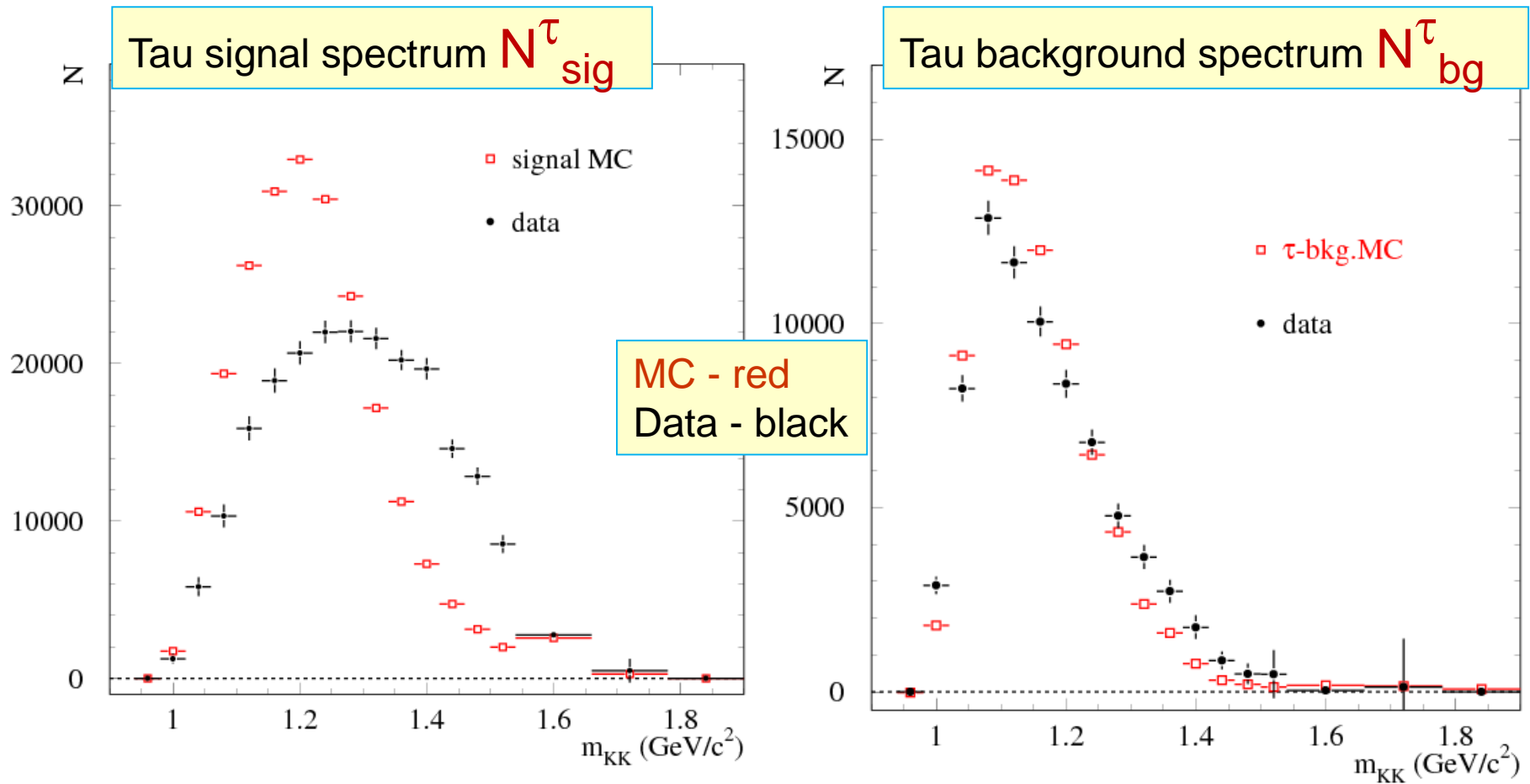
-  $\pi^0$  efficiency correction

- spurious photon correction

-  $0.984 = 1 - 0.024 * 0.68$

Fraction of events with  $\pi^0$

# The final $KK_S$ mass spectra for tau signal and background



## Branching fraction $\text{BF}(\tau^- \rightarrow \text{KK}_S \nu_\tau)$

$$\text{BF} = \frac{N_{\text{exp}}}{\text{LB}_{\text{lep}} \sigma_{\tau\tau}} = 0.740 \pm 0.011 \times 10^{-3} (\text{stat}) \pm 0.021 \times 10^{-3} (\text{syst})$$

$N_{\text{exp}} = (223741 \pm 3461)$  - total number of signal events,

$L = 468 \pm 2.5$  inv.fb,  $B_{\text{lep}} = 0.3521 \pm 0.0006$ ,  $\sigma_{\tau\tau} = 0.919 \pm 0.003$  nb

Total error (stat+syst) = 3.2%

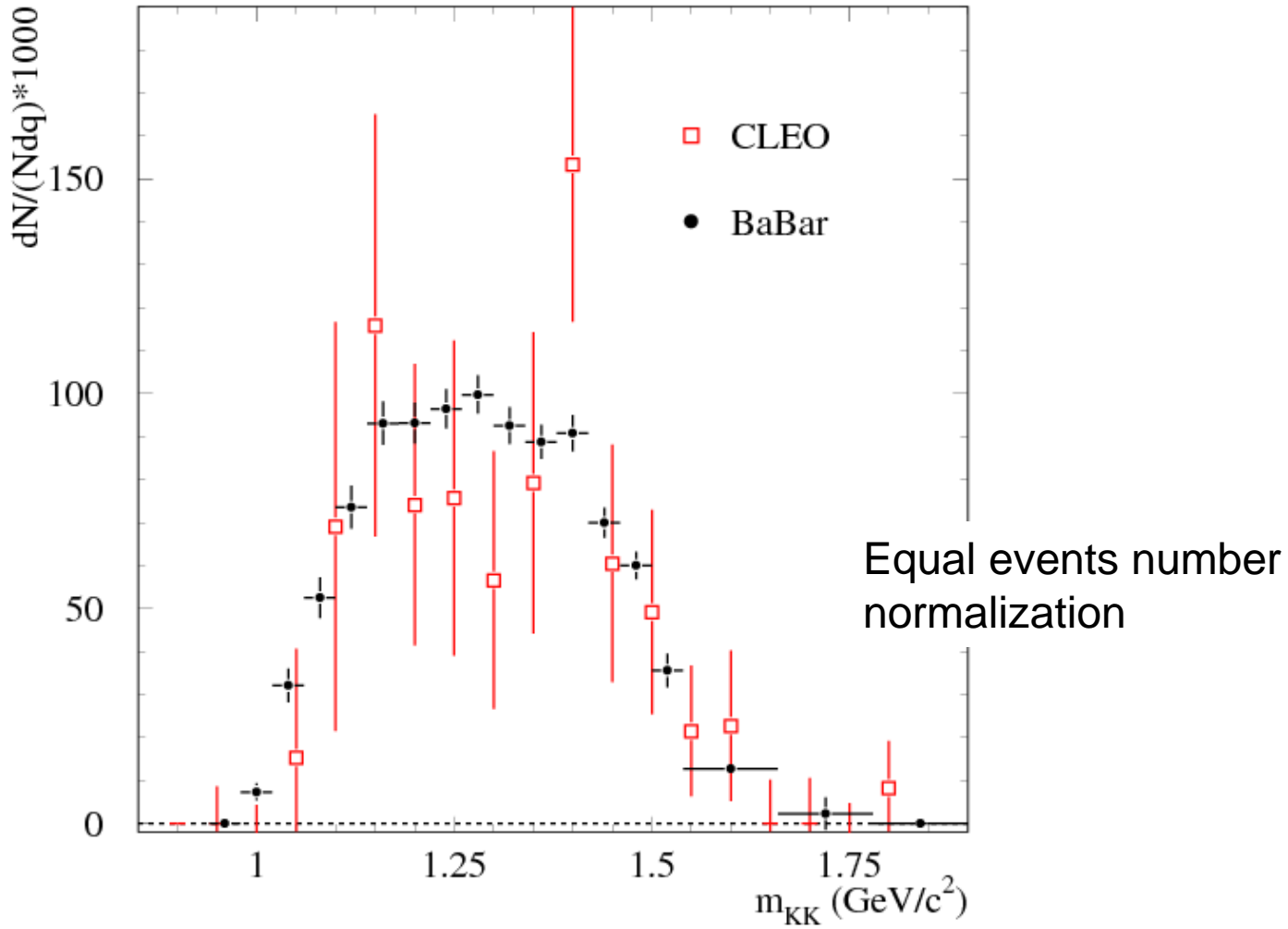
$\text{BF} (\text{PDG}_{2016}) = 0.740 \pm 0.025$

## Summary of systematic to $\text{BF}(\tau^- \rightarrow K_S K^- \nu_\tau)$

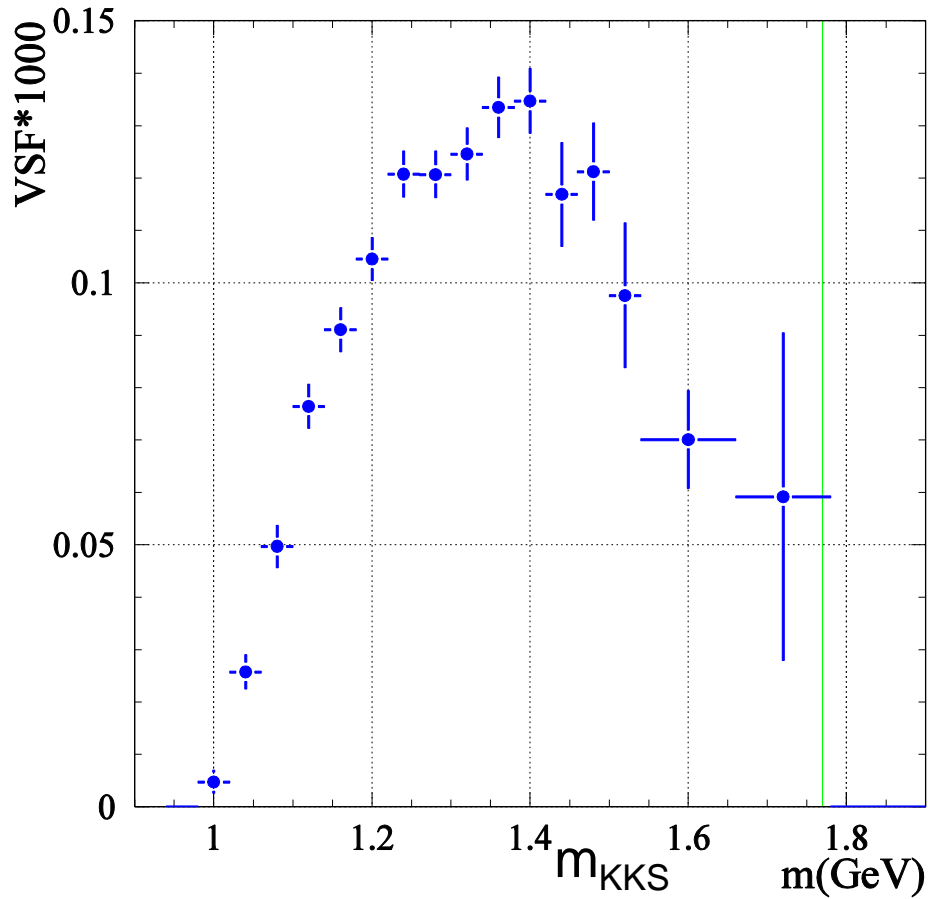
- 1 -  $K_S$  bkgd - 0.4%
- 2 - luminosity - 0.5%
- 3 - hadron bkgd subtr, - 0.5%
- 4 - track efficiency - 1.0%
- 5 - PID - 0.5%
- 6 -  $\tau$  bkgd with  $\pi^0$  - 2.3%
- 7 -  $\tau$  bkgd without  $\pi^0$  - 0.3%

Total - 2.7%

# BaBar-CLEO $KK_S$ mass spectra comparison



Vector spectral function for  $\tau^- \rightarrow K_S K^- \nu_\tau$  process,  
- first measurement





## Заключение

1. В процессе  $\tau^- \rightarrow K_S K^- \nu_\tau$  измерен массовый спектр  $K_S K^-$  системы с точностью значительно лучше чем в предыдущих измерениях
2. Измеренная вероятность распада  $\tau^- \rightarrow K_S K^- \nu_\tau$  хорошо согласуется со среднемировым значением
3. Впервые построена векторная спектральная функция распада  $\tau^- \rightarrow K_S K^- \nu_\tau$ .

To be submitted to Phys.Rev. D, rapid communication

